

# PSO with Robust Disturbance Rejection Controller for Maneuvering Control the Altitude of UAV

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## **Abstract**

*In this research article, particle swarm optimization (PSO) algorithm with variable weights and robust disturbance rejection (RDR) controller used to control the height of unmanned aerial vehicle (UAV). To solve the problem of controller parameters and robustness in obtaining a set of optimal solutions for the attitude control movements of the quadrotor UAV. The algorithm designed in this article is mainly composed of two parts; the first one in accordance with the iterative process, the distance of swarm particles with the variable weight of the dynamic change in the particle size of the global optimum set the coefficient to control its impact on the degree of inertial weight. The global optimal value of the result shows that the optimization algorithm is effective to adjust the parameters of the designed controller, which in result guarantee the quality in the control of the UAV and improve the design efficiency.*

**Keywords:** UAV, Algorithm, Quadrotor.

## **1. Introduction**

Unmanned aerial vehicles (UAVs), commonly known as drones, have found a wide range of applications during the past few years due to their low cost, efficiency and high mobility. UAVs have generally used in the military, deployed in remote and hostile areas where they perform their operations without endangering pilot lives. In the present era, these aircrafts are in high demand because they are much safer and more convenient than traditional aircrafts [1] and [2]. UAVs generally classified into two types based on their weight lifting capacity, engine type, range and maximum altitude etc. The first one fixed wing, these aircraft usually have high speed but they could only fly in continuous motion because of fixed mechanical structure. Second, one is the rotary wing aircraft such as UAVs; they are able to fly in any direction stand stationary in the air, able to hold on specific altitude in the air [3]. In reference [4] fuzzy PID controller and PID controller discussed, which plays an important role in achieving the stable attitude angle control of the aircraft, but there are some limitations that it has poor adaptability and can use for indoor flight operations. There is a huge demand of anti-interference control technology, where the aircraft requires high control accuracy and faces tremendous external interferences that provides stable and better flights

results. Such as in reference [5], in order to minimize the air interferences and wind turbulences a self-immunity controller designed.

In reference [6] a cascade system of proportional derivative and active disturbance control proposed. In that controller the parameters of outer loop is control by PD controller and inner loop controlling done by ADRC. The use of PD control structure is easy and simple whereas Adaptive disturbance rejection controller (ADRC) has strong decoupling ability to minimize the internal and external interference. In reference [7] the theories of higher order sliding mode observer (HSMC) introduced in the ADRC which in result improved the ADRC, so that the controller has better control effects. Although there are several advantages of the ADRC like the accurate mathematical, model which is independent of the object, enhanced ability to estimate and compensate the uncertainties. However, there is no proper parameters for the tuning methods, using artificial error methods to make an efficient control system of the aircraft [8]. In reference [9] the parameters of adaptive disturbance rejection controller using particle swarm optimization PSO were discussed. On the other hand, there are some issues of local optimization and slow convergence in the standard particle swarm algorithm. By adjusting ADRC controller parameter of the quadrotor UAV using the variable weight hybrid particle swarm optimization algorithm the above problems can be resolved [10]. The whole article comprised of the following sections. Section I of the paper consists of an introduction, in section II the modelling of the UAV discussed. The adaptive disturbance rejection controller defined in section III of this paper. In section IV the improved particle swarm optimization algorithm is discussed. The complete article concluded in section V of this paper.

## 2. Modelling of the UAV

The dynamics of the quad-rotor aircraft used for the mathematical modelling and the kinematic equation of Euler angles of the UAV taken from [11] and [12];

$$\begin{aligned}
 \ddot{x} &= \frac{(\cos\phi\sin\theta\cos\psi + \sin\phi\sin\psi) * u_1}{m} \\
 \ddot{y} &= \frac{(\cos\phi\sin\theta\sin\psi + \sin\phi\cos\psi) * u_1}{m} \\
 \ddot{z} &= -g + \frac{(\cos\phi\cos\theta) * u_1}{m} - g \\
 \ddot{\phi} &= \dot{\theta}\dot{\psi} \left( \frac{I_y - I_z}{I_x} \right) + \frac{1u_2}{I_x} \\
 \ddot{\theta} &= \dot{\phi}\dot{\psi} \left( \frac{I_z - I_x}{I_y} \right) + \frac{1u_3}{I_y} \\
 \ddot{\psi} &= \dot{\phi}\dot{\theta} \left( \frac{I_x - I_y}{I_z} \right) + \frac{1u_4}{I_z}
 \end{aligned} \tag{01}$$

In equation (1)  $x, y, z$  are the geographic coordinate system of the quadrotor UAV also known as Earth coordinates,  $\phi, \theta, \psi$  are coordinate positions under reference coordinate system defined as roll angle, pitch angle and yaw angle. The  $I_x, I_y, I_z$  are the three moments of inertia around  $x, y, z$  axes,  $g$  is the acceleration due to gravity of the aircraft,  $m$  is defined as the quality of the aircraft  $u_1, u_2, u_3, u_4$  for the system control amount, the relationship with the quadrotor speed parameters as follows:

$$\begin{aligned}
 u_1 &= k_t(\mu_1^2 + \mu_2^2 + \mu_3^2 + \mu_4^2) \\
 u_2 &= k_t(\mu_1^2 - \mu_3^2) \\
 u_3 &= k_t(\mu_2^2 - \mu_4^2) \\
 u_4 &= k_d(\mu_1^2 - \mu_2^2 + \mu_3^2 - \mu_4^2)
 \end{aligned} \tag{02}$$

### 3. Robust disturbance rejection controller

The quadrotor robust disturbance controller define by the second order tracking differentiator TD, arrange the transition process, according to the set value  $y_d$  arrange the transition process  $y_{d1}$  and extract the differential signal  $y_{d2}$ .

$$\{e = y_{d1} - y_d y_{d1} = y_{d1} + h y_{d2} y_{d2} = y_{d2} + h g s t(e, y_{d2}, r, h_0) \tag{03}$$

In equation (3),  $h$  is the step, the  $h_0$  and  $h$  are independent factors which has a filtering effect also called as the filter factor. The  $r$  determines the tracking speed of the input signal differentiator, known as speed factor,  $g s t$  function is the most rapid control function which is;

$$u = g s t(y_1, y_2, r, h) \tag{04}$$

According to controlled object, the expanded state observer ESO input  $u_1$  and output  $y$ . The estimated state of controlled objects  $Z_1$ ,  $Z_2$  and the total amount of disturbance by the object  $Z_3$ .

$$\begin{aligned}
 \{e = Z_1 - y \geq g a l(e, \alpha_1) g e_1 = g a l(e, \alpha_2) Z_1 = Z_1 + h(Z_2 - \gamma_{01} e) Z_2 \\
 = Z_2 + h(Z_3 - \gamma_{02} \geq + b u) Z_3 = Z_3 + h(-g e_1)
 \end{aligned} \tag{05}$$

In equation (5)  $\gamma_{01}$ ,  $\gamma_{02}$  are greater than zero and require a proper adjustment of the parameter,  $0 < \alpha_1, \alpha_2 < 1$  usually take  $\alpha_1 = 0.5$ ,  $\alpha_2 = 0.25$ ,  $b$  is a constant,  $g a l$  is the function of linear range width. The function of  $g a l$  is defined as:

$$g a l(e, \alpha) = \{|e|^\alpha \cdot \text{sign}(e), 0 \tag{06}$$

In equation (6) the value of  $\alpha$  is taken as 0.5. Nonlinear error feedback law, according to the input to in  $e_1$ ,  $e_2$  and  $Z_3$  in order to determine the final amount of controlled object  $u_1$ .

$$\{e_1 = y_{d1} - Z_1 e_2 = y_{d2} - Z_2 u_{10} = \gamma_1 g a l(e_1, \alpha_1) + \gamma_2 g a l(e_2, \alpha_2) u_1 = u_{10} - \frac{Z_3}{b} \tag{07}$$

In equation (7) the  $g a l$  function definition is same as defined in equation (6), but the value of  $\alpha$  is different, in order to achieve good robustness and adaptability in the controller select the appropriate parameters  $\gamma_1$  and  $\gamma_2$ .

### 4. Particle swarm optimization

The particle swarm optimization (PSO) is an optimization algorithm. Each particle of particle swarm optimization. It provides a possible set solution, which provides

ultimate solution of the problems. By interacting with other particles, in order to find the optimal solution to the problem it constantly update itself with the status information of the entire population [13-15].

The particle group in N dimensional space consisting on M particles, here  $X_i = x_{i1}, x_{i2}, x_{i3}, x_{i4}, \dots, x_{in}$  represents the  $i_{th}$  position of a particle in the  $n_{th}$  dimensional space.  $V_i = (v_{i1}, v_{i2}, v_{i3}, \dots, v_{in})$  here  $v$  represents the  $i_{th}$  particle speed of  $P_g = (p_{g1}, p_{g2}, p_{g3}, p_{g4}, \dots, p_{gn})$ .

Each particle in PSO continuously update its velocity and position in space in an iterative process by its own population optimal values as shown in equation (9) and (10).

$$V_{kd}^{k+1} = \omega V_{kd}^k + c_1 r_1 (P_{id}^k - X_{id}^k) + c_2 r_2 (P_{gd}^k - X_{id}^k) \quad (08)$$

$$X_{id}^{k+1} = X_{id}^k + V_{id}^{k+1} \quad (09)$$

In equation (9), (10)  $\omega$  is the inertial weight;  $d=1,2,3, \dots, n$ ;  $i=1,2,3, \dots, m$ ;  $c_1, c_2$  is the acceleration factor, whose value is greater than zero.  $r_1, r_2$  is a random number distributed in the interval of 0, 1;  $k$  is defined as number of current iterations.

The  $\omega$  defines the inertial weights which reflects the velocity of the particles that has the same previous ability.  $Y$  presents linear decrement inertia weights, as shown in equation (10), if the inertia weight value is large it favors global search, while the smaller inertia weight value is more conducive to local search.

In below equation the inertial weight  $\omega$  used to define the velocity of the particle.

$$\omega(k) = \frac{\omega_{max} - k(\omega_{max} - \omega_{min})}{T_{max}} \quad (10)$$

Where  $\omega_{max}$  and  $\omega_{min}$  for the maximum and minimum inertia weight value,  $T_{max}$  is the maximum number of iterations.

#### 4.1. Improved basic flow of particle swarm algorithm

1. In order to select maximum history and optimal particles set the position and velocity of all particles as per the fitness function value criteria.
2. Calculate the distance between each particle and the current global optimal position, get  $L_{ki}$  max,  $L_{ki}$  min from equation (8) update the inertia weight of each particle in next iteration  $\omega$ .
3. According to equation (8), (9), (10), update the position and velocity of each particle and calculate the fitness value.
4. The current value replaces the historical optimal value, if the current fitness value of the particle is better than its historical optimal value.
5. Replace the global optimal value, if the particle is better than the global historical optimal value.

6. Determine whether the hybridization conditions that are continuous  $H$  generation global optimal value remains unchanged, in the implementation of step 7.
7. Determine whether the termination condition is satisfied, the output is global optimal, otherwise step 2.

#### 4.2. Particle swarm algorithm RDR controller

The mathematics of the quadrotor aircraft build in MATLAB/Simulink aircraft simulation model and design *RDR* controller pair *UAV* height and three-attitude angles to control. By combining *RDR* controllers with improved particle swarm optimization (PSO), select the maximum impact on the performance of *RDR* six parameters, using particle swarm optimization tuning, which *ESO* take  $\gamma_{01}$ ,  $\gamma_{02}$ ,  $\gamma_1$ ,  $\gamma_2$  and  $b$  such as shown in figure 1 below.

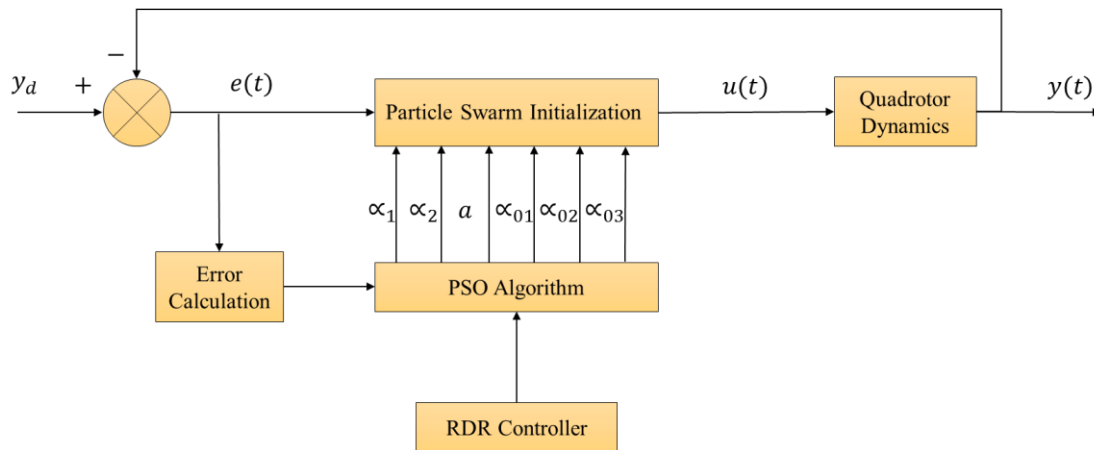


Figure: 1 Error performance indicators

#### 5. Simulation results analysis

In this part of the manuscript, the robustness of the designed controller is defined. The parameters of quadrotor UAV is defined in table 1, and table 2 of this article contains PSO-RDR initialization parameters. The overall simulation model divided into two groups one is the altitude curve and the other one is no. of iterations for optimization. From figure 2, it shows the altitude curve of the UAV in which it can be clearly seen that in a 25 second time period, the combination of PSO-RDR perform better in achieving the reference height of 4.5 meters as compared to the traditional PSO controller. Although it can also observe from the simulated result that designed controller has better robustness and quick convergence speed.

Similarly, figure 3 shows that standard particle swarm optimization algorithm converges after 4 iterations, while the robust disturbance rejection based PSO algorithm converges after about 3 iterations this conclusion also shows the quick convergence response of the designed controller.

Table 1: Quadrotor Parameters

Parameters	Values	Units
$m$	0.888	$kg$
$l$	0.2335	$m$
$I_x$	0.01896	$kg.m^2$
$I_y$	0.01896	$kg.m^2$
$I_z$	0.00939	$kg.m^2$

Table 2: Improved PSO Initialization Parameter

Parameters	Values	Parameters
$\omega_{max}$	0.9	$\omega_{max}$
$\omega_{min}$	0.4	$\omega_{min}$
$c_1, c_2$	2	$c_1, c_2$
Particle swarm size	20	Particle swarm size
Number of iterations	50	Number of iterations
$h$	10	$h$

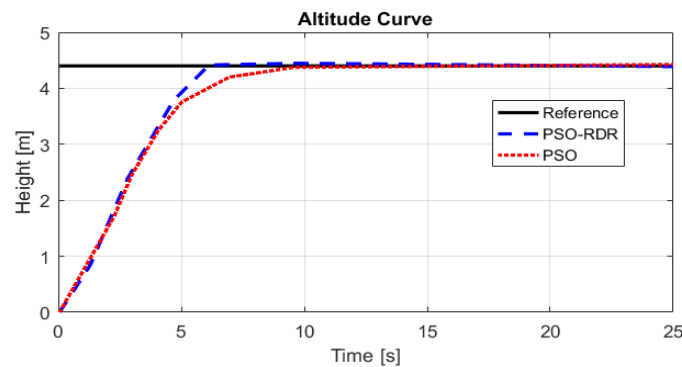


Figure: 2 Height control curve of UAV

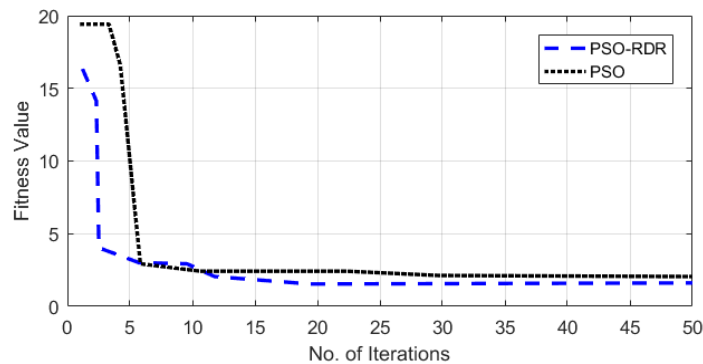


Figure: 3 No. of iterations for optimization

## 5. Conclusion

To conclude this article, it is observed that the designed PSO-RDR controller have better convergence speed for maneuvering control the altitude of UAV. To prove the efficiency of the proposed controller the results of both the standard PSO controller and robust disturbance rejection based PSO are compared in Simulink simulations, which

shows the effectiveness of the designed controller. It can achieve precise and fast control of the height and attitude of the aircraft to improve the efficiency of flight control designed system.

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